

Statistics
Fall 2021
Lecture 29



Comparing Two Population standard deviations

Sample 1	Sample 2
S_1	S_2
n_1	n_2

σ_1 & σ_2 :

$$H_0: \sigma_1 = \sigma_2$$

$$H_1: \sigma_1 \neq \sigma_2 \quad \text{TTT}$$

CTS F

\Rightarrow 2-Samp F Test

P-value P

Proceed with Testing chart

Final Conclusion.

$$S_1 > S_2$$

$$Ndf = n_1 - 1$$

$$Ddf = n_2 - 1$$

$$\text{CTS } F = \frac{S_1^2}{S_2^2}$$

Consider the chart below

Sample 1	Sample 2
$S_1 = 8$	$S_2 = 5$
$n_1 = 10$	$n_2 = 7$

① Verify $S_1 > S_2$ ✓

② Find CTS $F = \frac{S_1^2}{S_2^2}$

$$F = \frac{8^2}{5^2} = 2.56$$

③ Test the claim that $\sigma_1 = \sigma_2$ using $\alpha = .02$.

$H_0: \sigma_1 = \sigma_2$ claim

$H_1: \sigma_1 \neq \sigma_2$ TTT

CTS $F = 2.56$

P-value $P = .265$

Using P-Value only

P-value $> \alpha$

H_0 valid
 H_1 invalid

STAT TESTS

2-Samp F Test

Inpt: STATS

$S_1 = 8$ $n_1 = 10$

$S_2 = 5$ $n_2 = 7$

$\sigma_1 \neq \sigma_2$ Calculate

valid claim

Fail-to-reject the claim

Exam 1:	$n = 8$	$S = 10$
Exam 2:	$n = 12$	$S = 15$

$H_0: \sigma_1 = \sigma_2$

$H_1: \sigma_1 \neq \sigma_2$ claim, TTT

Use $\alpha = .1$ to test the claim that two population standard deviations are not equal.

Exam 2	Exam 1
$n_1 = 12$	$n_2 = 8$
$S_1 = 15$	$S_2 = 10$
$S_1 > S_2$	

$$CTS F = \frac{S_1^2}{S_2^2} = \frac{15^2}{10^2} = 2.25 \checkmark$$

$$Ndf = 12 - 1 = 11$$

$$Ddf = 8 - 1 = 7$$

2-Samp F Test

CTS $F = 2.25$

P-value $P = .291$

P-value method only:

P-value $> \alpha$

H_0 valid $\hat{=}$ H_1 invalid

invalid claim

Reject the claim

I randomly selected 10 female students, and standard deviation of their ages was 18 yrs. Females: $n=10, S=18$

I also randomly selected 15 male students, and standard deviation of their ages was 4 yrs. Males: $n=15, S=4$

Test the claim that two pop. standard deviations are equal. $\alpha = 0.05$

$H_0: \sigma_1 = \sigma_2$ claim
 $H_1: \sigma_1 \neq \sigma_2$ TTT

Females	Males
$n_1=10$	$n_2=15$
$S_1=18$	$S_2=4$
$S_1 > S_2$	

Ndf = 10-1 = 9
Ddf = 15-1 = 14

CTS $F = \frac{S_1^2}{S_2^2} = \frac{18^2}{4^2} = 20.25$

CTS $F = 20.25$
P-value $P = 3.05 \times 10^{-6}$
P-value $3 \times 10^{-6} < 0.05$
 $0.000003 < 0.05$

2-Samp F Test

P-value $< \alpha$
 H_0 invalid \rightarrow Invalid claim
 H_1 valid \rightarrow Reject the claim

Comparing at least 3 population means:

$H_0: \mu_1 = \mu_2 = \mu_3 = \dots = \mu_k$

H_1 : At least one mean is different. RTT

$k \rightarrow$ # of groups

\Rightarrow Ndf = $k-1$

$n \rightarrow$ Total Sample Size

\Rightarrow Ddf = $n-k$

CTS $F =$

\Rightarrow STAT TESTS

ANOVA(L1, L2, L3, ...)

Use Testing chart, and p-value method to proceed.

Name of the method
Analysis of Variance

ELAC		Mt. SAC		Chaffey	
23	28	19	25	26	32
32	45	34	40	40	35
18	35	48	28	20	
		30			

$K=3$
 $n=6+7+5=18$
 $df=k-1=2$
 $DfE=n-k=15$

Use $\alpha=.02$ to test the claim ELAC \rightarrow L1
 that all pop. means are equal. Mt. SAC \rightarrow L2
 Chaffey \rightarrow L3

$H_0: \mu_1 = \mu_2 = \mu_3$ claim
 $H_1: \text{At least one mean is different. RTT}$

STAT TESTS \uparrow ANOVA L1, L2, L3 Enter
 2nd 1 2nd 2 2nd 3

CTS F = .071
 P-value P = .931

$P\text{-value} > \alpha$
 $.931 > .02 \Rightarrow H_0 \text{ valid} \rightarrow \text{Valid claim}$
 $H_1 \text{ invalid} \rightarrow \text{FTR the claim}$

If we choose $\alpha = .932$, then
 $P\text{-value} \leq \alpha \Rightarrow H_0 \text{ invalid} \rightarrow \text{invalid claim}$
 $.931 \leq .932 \Rightarrow H_1 \text{ valid} \rightarrow \text{Reject the claim}$

I randomly selected exams from 4 different classes. Here are the scores:

L1 Morning class			L2 Afternoon class			L3 Evening class		L4 Weekend class	
78	85	93	88	95	62	74	65	76	70
68	100	80	75	80	100	86	68	80	
90	70			90	94	50	55		

$K=4$
 $n=8+5+6+6=25 \Rightarrow df=k-1=3$ Factor
 $DfE=n-k=21$ Error

Use $\alpha=.1$ to test the claim that not all Pop. means are the same.

$H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4$ claim
 $H_1: \text{At least one pop. mean is different. RTT}$

Morning \rightarrow L1
 Afternoon \rightarrow L2
 Evening \rightarrow L3
 Weekend \rightarrow L4

STAT TESTS ANOVA(L1, L2, L3, L4) Enter
 CTS F = 2.922
 P-value P = .058

P-value method only:
 $P\text{-value} < \alpha$
 $.058 < .1 \Rightarrow H_0 \text{ invalid}$
 $H_1 \text{ valid}$
 Valid claim \Rightarrow FTR The claim

to reject the claim
 $P\text{-value} > \alpha$
 $.058 > \alpha$

we need α to be
 $.05, .04, .03, .02, \text{ or } .01$

ANOVA does not tell us which mean is different.